

# Algebra 1

## HW 4 (Due: 14-09-2023)

1. Solve Exercise 27, Section 10.3, Dummit and Foote (This says free modules over non-commutative rings need not have unique rank)
2. Exercises 2, 5, 6 Section 10.4, Dummit and Foote
3. Show that the  $\mathbb{Z}$ -module  $\mathbb{Q}$  is not projective but is flat
4. Show that any  $R$ -module is contained in an injective  $R$ -module
5. Show that given a ring  $R$ , the statement that every  $R$ -module is projective is equivalent to the statement that every  $R$ -module is injective
6. Exercise 10, 11 Section 10.5, Dummit and Foote
7. Exercise 21, 23 Section 10.5, Dummit and Foote
8. (Optional Bonus problem + 10 points): Exercise 26, Section 10.5, Dummit and Foote